

I { X = random variable describing execution time

$$\text{exptime}(m) = E[X] = \sum_i x_i \cdot p_i$$

x_i = nb. of execution steps of the algorithm

p_i = probability that the number of executed steps in the algorithm is x_i

In case of deterministic algorithms, p_i = the probability of receiving an input such that the number of executed steps is x_i

II { For the seminar, we will also need the concept of indicator random variable.

Let X be a random indicator variable. $X = \begin{cases} 1, & \text{with prob } p \\ 0, & \text{with prob } 1-p \end{cases}$

III { Reminder: $E[X+Y] = E[X] + E[Y]$

1) More general: $E[\sum_i X_i] = \sum_i E[X_i]$

2) $E[a \cdot X] = a \cdot E[X]$, $a \in \mathbb{R}$ (a is a constant)

3) $E[X \cdot Y] = E[X] \cdot E[Y]$ iff X & Y are independent

$E[X] = 1 \cdot p + 0 \cdot (1-p) = p$ iff X is an indicator variable